

# PhyzGuide: Rotational Dynamics I

<b>translational</b>	<b>F O R C E</b>	<b>rotational</b>
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**Name** Force  
**Symbol**  $F$  (or  $\mathbf{F}$  vector)  
**Defn** Defined by Newton's second law:  
 $\Sigma F = ma$  ( $\Sigma \mathbf{F} = m\mathbf{a}$ )  
 Force is what causes linear acceleration—change in linear velocity.

**Name** Torque  
**Symbol**  $\tau$  ( $\tau$  vector)  
**Defn** Torque is the rotational version of force. It causes angular acceleration—change in angular velocity. It is defined algebraically as:

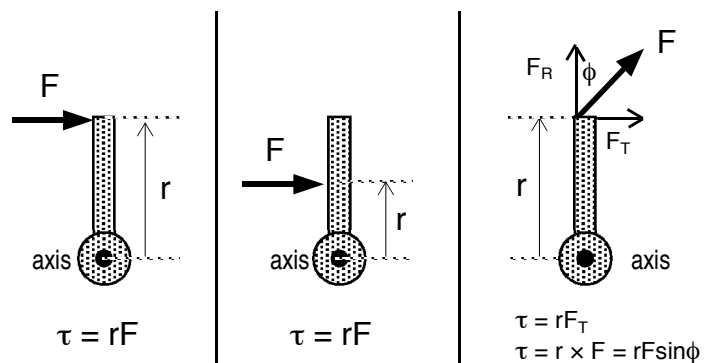
$$\tau = rF\sin\phi = rF \text{ when } \mathbf{r} \perp \mathbf{F}.$$

$r \equiv$  The *distance* from the axis of rotation to the point through which the force is acting. (Notice that a force exerted at a point far from the axis of rotation produces a greater torque than the same force exerted near the axis.) This distance is sometimes called the **lever arm**, or **torque arm**.

$F \equiv$  The quantity of linear *force* acting.

$\phi \equiv$  The *angle* between the radial direction and the direction of force.

NOTE:  $F_T$  is the component of force in the TANGENTIAL direction,  $F_R$  is the component of force in the RADIAL direction.



**Name** Mass

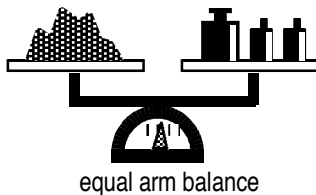
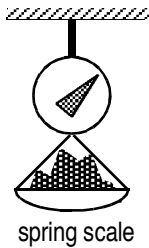
**Symbol**  $m$

**Defn** A measure of resistance to change in linear velocity.

HOW TO FIND IT:

Gravitational Method: Weigh the object and calculate mass via the relation  $W = mg$

Inertial Method: Inertial balance



GRAVITATIONAL METHODS

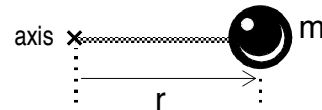
**Name** Rotational Inertia, also Moment of Inertia

**Symbol**  $I$  (capital “ $i$ ”)

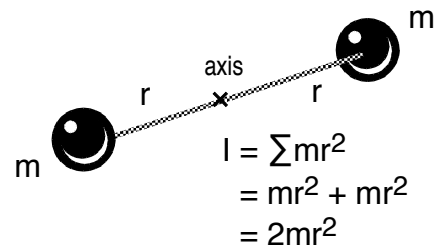
**Defn** A measure of resistance to change in angular velocity.

HOW TO FIND IT:

In general,  $I = \sum mr^2$ . For a point mass  $m$ , rotating at a distance  $r$  from an axis,  $I = mr^2$ . (This distance is called the **moment arm**.) Solid objects vary—use tables giving  $I$  in terms of total mass  $M$  and radius  $R$  of an object.



$$I = mr^2$$



$$\begin{aligned} I &= \sum mr^2 \\ &= mr^2 + mr^2 \\ &= 2mr^2 \end{aligned}$$

### NEWTON'S FIRST LAW

Bodies maintain their state of rest or of constant speed in a straight line unless acted on by an unbalanced external force.

### NEWTON'S SECOND LAW

Acceleration is proportional to net force and inversely proportional to mass:  
 $\Sigma \mathbf{F} = m\mathbf{a}$ .

### NEWTON'S THIRD LAW

“For every force there is an equal and opposite reaction force.” Forces always come in equal and opposite pairs.

### NEWTON'S FIRST LAW

Bodies maintain their state of rest or of constant angular speed in the same plane unless acted on by an unbalanced external torque.

### NEWTON'S SECOND LAW

Angular acceleration is proportional to net torque and inversely proportional to rotational inertia:  $\Sigma \tau = I\alpha$ .

### NEWTON'S THIRD LAW

“For every torque there is an equal and opposite reaction torque.” Torques always come in equal and opposite pairs.